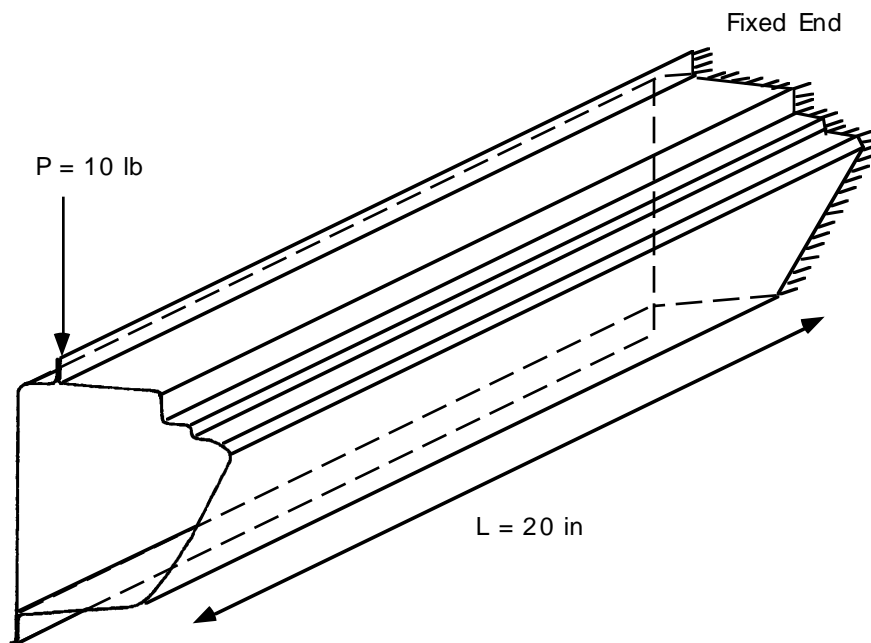




2. Assuming the cross section given in 1-(a), we consider a cantilever beam shown in the following figure.



Although this cantilever should be regarded as a short beam, assuming that this is modeled as a beam we have studied so far,

- (a) Find the axial stress distribution on the cross section at the fixed end of the cantilever, and
- (b) Find the horizontal and vertical deflections as well as the angle of twist of the beam at the free end.

To do so, you may model this cantilever by a beam element. Since the one end is fixed, you will end up a 6×6 matrix equation that can be solved by MATLAB. Unknowns are the two transverse deflections of the shear center, the average axial displacement, three rotations about the x , y , and z axes, respectively, where x and y are the principal axes of the cross section. For your analysis, you should specify what material constants are applied for structural steel. Here, we expect that Young's modulus is about 200 Gpa (30 M psi), and Poisson's ratio is about 0.29.

It is also noted that the vertical load P is applied not on the shear center, it generates twist moment about the shear center. Thus, you will have three input, say, V_x , V_y , and M_z .