## HOMEWORK 2.

1.: A company holds 1.2 billion Japanese Yen, 10.5 billion Indonesian rupiahs, and 28 million Malaysian ringgits. Here are the exchange rates and transaction costs. JY = Japanese Yen, IR = Indonesian Rupiah, $\mathrm{MR}=$ Malaysian Ringgit, UD $+\mathrm{US} \$, \mathrm{CD}=$ Canadian\$, $\mathrm{EE}=$ European Euro, $\mathrm{EP}=$ English Pound, MP $=$ Mexican Peso.

| From | Exchange Rate to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JY | IR | MR | UD | CD | EE | EP | MP |
| JY | 1 | 50 | 0.04 | 0.008 | 0.01 | 0.0064 | 0.0048 | 0.0768 |
| IR |  | 1 | 0.0008 | 0.00016 | 0.0002 | 0.000128 | 0.000096 | 0.001536 |
| MR |  |  | 1 | 0.2 | 0.25 | 0.16 | 0.12 | 1.92 |
| UD |  |  |  | 1 | 1.25 | 0.8 | 0.6 | 9.6 |
| CD |  |  |  |  | 1 | 0.64 | 0.48 | 7.68 |
| EE |  |  |  |  |  | 1 | 0.75 | 12 |
| EP |  |  |  |  |  |  | 1 | 16 |
| MP |  |  |  |  |  |  |  | 1 |


| From | Transaction cost \% |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JY | IR | MR | UD | CD | EE | EP | MP |
| JY |  | 0.5 | 0.5 | 0.4 | 0.4 | 0.4 | 0.25 | 0.5 |
| IR |  |  | 0.7 | 0.5 | 0.3 | 0.3 | 0.75 | 0.75 |
| MR |  |  |  | 0.7 | 0.7 | 0.4 | 0.45 | 0.5 |
| UD |  |  |  |  | 0.15 | 0.2 | 0.2 | 0.2 |
| CD |  |  |  |  |  | 0.2 | 0.1 | 0.1 |
| EE |  |  |  |  |  |  | 0.05 | 0.5 |
| EP |  |  |  |  |  |  |  | 0.5 |
| MP |  |  |  |  |  |  |  |  |

(i): Formulate the problem of finding the most cost effective method to convert these holdings into US\$ as a min cost flow problem.
(ii): Suppose there are transaction limits for converting Yen, Rupiah, and Ringgits (only these currencies, no limits for converting other currencies) as shown in the following table (unit = equivalent of UD1000,000). Then find the most cost effective way of converting as much of these currency holdings into US\$ as possible.

| From | Transaction Limits |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JY | IR | MR | UD | CD | EE | EP | MP |
| JY |  | 5 | 5 | 2 | 2 | 2 | 4 | 8 |
| IR | 5 |  | 2 | 1 | 2 | 1 | 3 | 2 |
| MR | 3 | 5 |  | 2 | 3 | 3 | 2 | 1 |

2: There are 10 cities, we will denote them by SP, K, P, U, M, SAM, O, SAR, Y, R. Among these $M$ is going to be the headquarters for a multinational company. The company has already established communication links between pairs (M, SP), and (M, R).

Each communication link joining a pair of cities serves for communication both ways.
The company wants to establish communication links between $M$ and the remaining 7 cities at minimum cost. Two cities can communicate as long as there is a path between them.

It is possible to establish a communication link between the following pairs of cities with the associated costs (unit $=\$ 100,000$ ) as shown in the following table.

| Pair | Cost | Pair | Cost | Pair | Cost |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (SP, K) | 210 | (R, SAR) | 200 | (P, U) | 125 |
| (SP, P) | 185 | (R, O) | 120 | (Y, U) | 125 |
| (SP, U) | 225 | (K, P) | 150 | (U, SAM) | 100 |
| (M, U) | 310 | (K, U) | 105 | (U, O) | 75 |
| (M, SAM) | 195 | (K, SAR) | 95 | (SAR, SAM) | 100 |
| (M, O) | 440 | (P, Y) | 85 | (SAR, O) | 95 |
| (M, SAR) | 200 |  |  |  |  |

It is required to determine which of these communication links be built to make sure that M can communicate with all the other cities at minimum cost. Formulate using a network model.

